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$$M_p = \begin{matrix} E_1 \\ E_2 \\ \vdots \\ E_S \\ E_{S+1} \\ \vdots \\ E_n \end{matrix} \begin{bmatrix} E_1 & E_2 & \cdots & E_S & E_{S+1} & \cdots & E_n \\ p_{1,1} & p_{1,2} & \cdots & p_{1,S} & p_{1,S+1} & \cdots & p_{1,n} \\ p_{2,1} & p_{2,2} & \cdots & p_{2,S} & p_{2,S+1} & \cdots & p_{2,n} \\ \vdots & \vdots & & \vdots & \vdots & & \vdots \\ p_{S,1} & p_{S,2} & \cdots & p_{S,S} & p_{S,S+1} & \cdots & p_{S,n} \\ p_{S+1,1} & p_{S+1,2} & \cdots & p_{S+1,S} & p_{S+1,S+1} & \cdots & p_{S+1,n} \\ \vdots & \vdots & & \vdots & \vdots & & \vdots \\ p_{n,1} & p_{n,2} & \cdots & p_{n,S} & p_{n,S+1} & \cdots & p_{n,n} \end{bmatrix} \quad (1)$$

$$I = \begin{matrix} E_1 \\ E_2 \\ \vdots \\ E_S \end{matrix} \begin{bmatrix} E_1 & E_2 & \cdots & E_S \\ P_{1,1} & P_{1,2} & \cdots & P_{1,S} \\ P_{2,1} & P_{2,2} & \cdots & P_{2,S} \\ \vdots & \vdots & & \vdots \\ P_{S,1} & P_{S,2} & \cdots & P_{S,S} \end{bmatrix} \quad (2)$$

$$O = \begin{matrix} E_1 \\ E_2 \\ \vdots \\ E_S \end{matrix} \begin{bmatrix} E_{S+1} & E_{S+2} & \cdots & E_n \\ P_{1,S+1} & P_{1,S+2} & \cdots & P_{1,n} \\ P_{2,S+1} & P_{2,S+2} & \cdots & P_{2,n} \\ \vdots & \vdots & & \vdots \\ P_{S,S+1} & P_{S,S+2} & \cdots & P_{S,n} \end{bmatrix} \quad (3)$$

:

$$R = \begin{matrix} E_{S+1} \\ E_{S+2} \\ \vdots \\ E_n \end{matrix} \begin{bmatrix} E_1 & E_2 & \cdots & E_S \\ P_{S+1,1} & P_{S+1,2} & \cdots & P_{S+1,S} \\ P_{S+2,1} & P_{S+2,2} & \cdots & P_{S+2,n} \\ \vdots & \vdots & & \vdots \\ P_{n,1} & P_{n,2} & \cdots & P_{n,S} \end{bmatrix} \quad (4)$$

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: M_p

$$M_P = \begin{matrix} & E_1 & E_2 & E_3 & E_4 & E_I & E_{II} \\ E_1 & \left[\begin{array}{cccccc} 0 & P_{1,2} & 0 & 0 & P_{1,I} & 0 \end{array} \right] \\ E_2 & \left[\begin{array}{cccccc} 0 & 0 & P_{2,3} & 0 & P_{2,I} & 0 \end{array} \right] \\ E_3 & \left[\begin{array}{cccccc} 0 & 0 & 0 & P_{3,4} & P_{3,I} & 0 \end{array} \right] \\ E_4 & \left[\begin{array}{cccccc} 0 & 0 & 0 & 0 & P_{4,I} & P_{4,II} \end{array} \right] \end{matrix} \quad (5)$$

:

$$\begin{matrix} & E_1 & E_2 & E_3 & E_4 \\ E_1 & \left[\begin{array}{cccc} 0 & P_{1,2} & 0 & 0 \end{array} \right] \\ E_2 & \left[\begin{array}{cccc} 0 & 0 & P_{2,3} & 0 \end{array} \right] \\ E_3 & \left[\begin{array}{cccc} 0 & 0 & 0 & P_{3,4} \end{array} \right] \\ E_4 & \left[\begin{array}{cccc} 0 & 0 & 0 & E_{4,4} \end{array} \right] \end{matrix} \quad (6)$$

:

$$Q = \begin{matrix} & E_{S+1} & E_{S+2} & \cdots & E_n \\ E_{S+1} & \left[\begin{array}{cccc} P_{S+1,S+1} & P_{S+1,S+2} & \cdots & P_{S+1,n} \end{array} \right] \\ E_{S+2} & \left[\begin{array}{cccc} P_{S+2,S+1} & P_{S+2,S+2} & \cdots & P_{S+2,n} \end{array} \right] \\ \vdots & \left[\begin{array}{cccc} \vdots & \vdots & \cdots & \vdots \end{array} \right] \\ E_n & \left[\begin{array}{cccc} P_{n,S+1} & P_{n,S+2} & \cdots & P_{n,n} \end{array} \right] \end{matrix} \quad (7)$$

:

$$(I-Q) = \begin{bmatrix} 1 & 0 & \cdots & 0 \\ 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & 1 \end{bmatrix} - \begin{bmatrix} P_{S+1,S+1} & P_{S+1,S+2} & \cdots & P_{S+1,n} \\ P_{S+2,S+1} & P_{S+2,S+2} & \cdots & P_{S+2,n} \\ \vdots & \vdots & \cdots & \vdots \\ P_{n,S+1} & P_{n,S+2} & \cdots & P_{n,n} \end{bmatrix} \quad (8)$$

:

$$(I - Q) = \begin{bmatrix} 0 & -P_{1,2} & 0 & 1 \\ 0 & 1 & -P_{2,3} & 0 \\ 0 & 0 & 0 & -P_{3,4} \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (9)$$

:

$$(I - Q)^{-1} = \begin{bmatrix} 1 & -P_{1,2} & 0 & 0 \\ 0 & 1 & -P_{2,3} & 0 \\ 0 & 0 & 1 & -P_{3,4} \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (10)$$

:

: 2006 1996

.2006 -1996 : (1)

13924	4859	3265	2599	3201	1997-1996
13020	4294	2813	2646	3267	1998-1997
12838	3743	3304	2451	3340	1999-1998
12621	3781	2214	2922	3704	2000-1999
12014	3310	3064	2720	2920	2001-2000
12674	3638	2912	2997	3127	2002-2001
15667	5201	3536	3497	3433	2003-2002
15623	5121	3950	3066	3486	2004-2003
13923	4160	3514	3085	3164	2005-2004
15971	5427	4145	3111	3288	2006-2005
138275	43534	32717	29094	32930	

. 4353

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.2006-1996

:(2)

1203	611	339	253	1997-1996
1817	911	622	284	1998-1997
1375	609	522	244	1999-1998
1268	758	297	213	2000-1999
1023	537	237	249	2001-2000
1071	421	377	273	2002-2001
1298	631	346	321	2003-2002
1355	506	454	395	2004-2003
1570	718	512	340	2005-2004
2053	785	839	429	2006-2005
14033	6487	4545	3001	

1403

(2)

:

$$100 \times \frac{\text{متوسط عدد الخريجين في السنة الواحدة}}{\text{متوسط عدد الطلاب السنة الرابعة}} = \quad (11)$$

$$100 \times \frac{1403}{4353} =$$

$$= 32\%$$

(3)

:

.2006-1996 : (3)

2234	553	689	505	487	1997-1996
1408	368	389	257	394	1998-1997
2872	1022	828	554	468	1999-1998
890	200	211	217	262	2000-1999
3658	1379	979	734	566	2001-2000
2836	1239	691	512	394	2002-2001
352	57	127	109	59	2003-2002
2960	1196	738	592	434	2004-2003
2257	1513	289	230	225	2005-2004
2618	1135	748	410	325	2006-2005
22085	8662	5689	4120	3614	
2208	866	569	412	361	

: (1)

$$\bar{N}_1 = \frac{32930}{10} = 3293 :$$

$$\bar{N}_2 = \frac{29094}{10} = 2909 :$$

$$\bar{N}_3 = \frac{32717}{10} = 3272 :$$

$$\bar{N}_4 = \frac{43537}{10} = 4353 :$$

: (3)

$$\bar{R}_1 = \frac{3614}{10} = 361 :$$

$$\bar{R}_2 = \frac{4120}{10} = 412 :$$

$$\bar{R}_3 = \frac{5689}{10} = 568.9 :$$

$$\bar{R}_4 = \frac{8662}{10} = 866.2 :$$

:

$$P_{1,1} = \frac{361}{3293} = 0.11 :$$

$$P_{2,1} = \frac{412}{2909} = 0.14 :$$

$$P_{3,1} = \frac{569}{3272} = 0.17 :$$

$$P_{4,1} = \frac{866}{4353} = 0.2 :$$

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$$P_{1,2} = 1 - P_{1,1} = 1 - 0.11 = 0.89$$

:

$$P_{1,3} = 1 - P_{2,1} = 1 - 0.14 = 0.86$$

:

$$P_{1,3} = 1 - P_{2,1} = 1 - 0.17 = 0.83$$

:

$$P_{4,II} = 1 - P_{4,1} = 1 - 0.2 = 0.8$$

:

$$M_p = \begin{matrix} & E_1 & E_2 & E_3 & E_4 & E_I & E_{II} \\ E_1 & \left[\begin{array}{cccccc} 0 & 0.89 & 0 & 0 & 0.11 & 0 \end{array} \right. \\ E_2 & \left[\begin{array}{cccccc} 0 & 0 & 0.86 & 0 & 0.14 & 0 \end{array} \right. \\ E_3 & \left[\begin{array}{cccccc} 0 & 0 & 0 & 0.83 & 0.17 & 0 \end{array} \right. \\ E_4 & \left[\begin{array}{cccccc} 0 & 0 & 0 & 0 & 0.2 & 0 \end{array} \right. \\ E_I & \left[\begin{array}{cccccc} 0 & 0 & 0 & 0 & 1 & 0 \end{array} \right. \\ E_{II} & \left[\begin{array}{cccccc} 0 & 0 & 0 & 0 & 0 & 1 \end{array} \right. \end{matrix} \quad (12)$$

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$$\begin{matrix} & E_1 & E_2 & E_3 & E_4 \\ E_1 & \left[\begin{array}{cccc} 0 & 0.89 & 0 & 0 \end{array} \right. \\ E_2 & \left[\begin{array}{cccc} 0 & 0 & 0.86 & 0 \end{array} \right. \\ E_3 & \left[\begin{array}{cccc} 0 & 0 & 0 & 0.83 \end{array} \right. \\ E_4 & \left[\begin{array}{cccc} 0 & 0 & 0 & 0 \end{array} \right. \end{matrix} \quad (13)$$

:

$$Q^0 + Q^1 + Q^2 + \dots \quad (14)$$

$$Q \quad Q^{0=1} :$$

:

$$Q^0 + Q^1 + Q^2 + \dots + \frac{1}{(1-Q)} = (1-Q)^{-1} \quad (15)$$

:

$$(I-Q) = \begin{matrix} & & I & & Q \\ \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right] & - & \begin{matrix} & & & \\ \left[\begin{array}{cccc} 0 & 0.89 & 0 & 0 \\ 0 & 0 & 0.86 & 0 \\ 0 & 0 & 0 & 0.83 \\ 0 & 0 & 0 & 0 \end{array} \right] & & \end{matrix} \end{matrix} \quad (16)$$

$$I - Q = \begin{bmatrix} 1 & -0.89 & 0 & 0 \\ 0 & 1 & -0.86 & 0 \\ 0 & 0 & 1 & -0.83 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (17)$$

$$N = (I - Q)^{-1} = \begin{bmatrix} 1 & 0.89 & 0.77 & 0.64 \\ 0 & 1 & 0.86 & 0.71 \\ 0 & 0 & 1 & 0.83 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (18)$$

$$I = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \quad (19)$$

$$(I - Q)^{-1} \cdot I = \begin{bmatrix} 1 & 0.89 & 0.77 & 0.64 \\ 0 & 1 & 0.86 & 0.71 \\ 0 & 0 & 1 & 0.83 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 3.3 \\ 2.57 \\ 1.83 \\ 1 \end{bmatrix} \quad (20)$$

:

P N

$$B = \begin{bmatrix} 1 & 0.89 & 0.77 & 0.64 \\ 0 & 1 & 0.86 & 0.71 \\ 0 & 0 & 1 & 0.83 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0.11 & 0 \\ 0.14 & 0 \\ 0.17 & 0 \\ 0.2 & 0.8 \end{bmatrix} = \begin{bmatrix} 0.49 & 0.51 \\ 0.43 & 0.57 \\ 0.34 & 0.66 \\ 0.2 & 0.8 \end{bmatrix} \quad (23)$$

%57

%51

%80

%66

2007 - 2006

2453

2865

3685

3897

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$$[2865 \ 2453 \ 3897 \ 3685] \quad (21)$$

:

B

$$[2865 \ 2453 \ 3897 \ 3685] \begin{bmatrix} 0.49 & 0.51 \\ 0.43 & 0.57 \\ 0.34 & 0.66 \\ 0.2 & 0.8 \end{bmatrix} \quad (22)$$

2948

1398 **2008**

2572 **2007**

1461 **2009**

. **2010**

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1. Derman C., Finite State Markovian Decision Process, Academic Press, New York,1970.
2. Bremaud Pierre, Markov Chains. Springer, New York, 2001.
3. Cyert R., Davidson H., Thompson G., "Estimation of the Allowance for Doubtful Accounts by Markov Chains", Management Science, Vol. 8,No.4, pp.287-303, 1963.
4. Fijins H.C., Stochastic Models: an Algorithmic Approach. Wiley, New York, 1994.
5. Grimmet G., Stirzaker D., Probability and Random Processes, 2nd sd., Oxford University Press, Oxford, 1992.
6. Kad E. PC., An Introduction to Stochastic Processes. Duxbury Press, Belmont, 1997.
7. Kallenberg O., Foundation of Modern Probability, Springer-Verlag, New Yprk, 1997.
8. Stewart W., Introduction to the Numerical Solution of Markov Chains, Princeton University Press, Princeton, NJ, 1995.