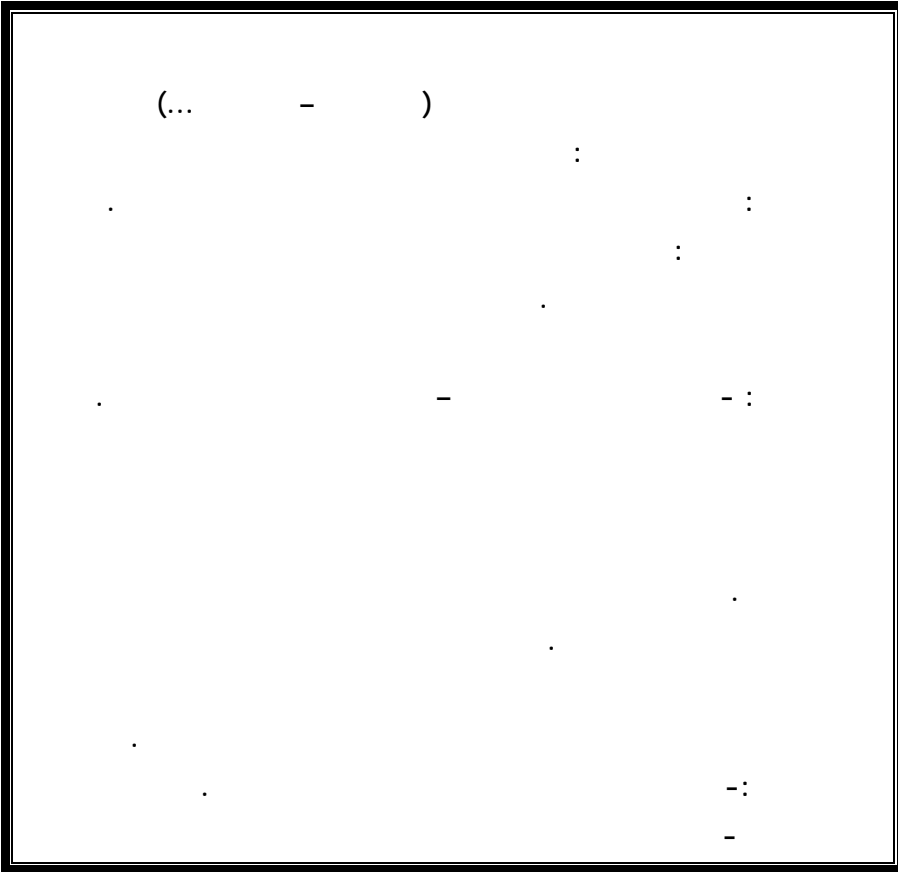


1



1

---

: -1

(*moment of elasticity*)

.( - - )

[1,2,3]

)

.(

: -2

( )

( $\xi$ )

.(matlab)

: -3

: -1-3

.(b-1)

[1,2]

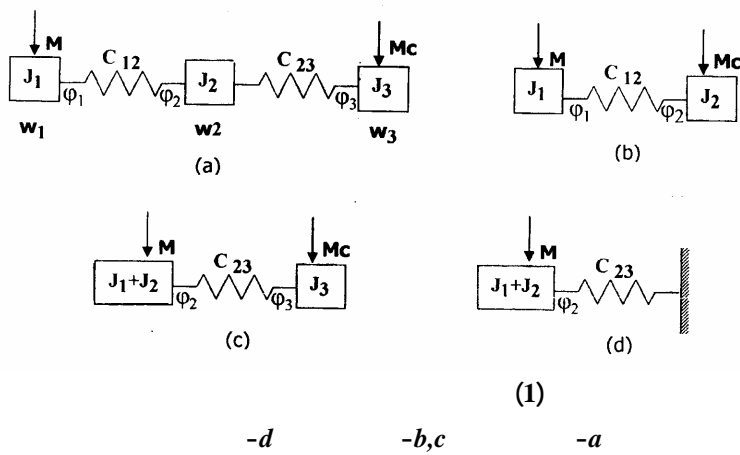
$M_C [N.m]$

(Moment of Elasticity)

:

$$M_Y = C_{12}(\varphi_1 - \varphi_2)$$

( 1 )



[1,

:4,5]

$$\left. \begin{aligned}
 M_1 - M_Y &= J_1 \frac{d^2 \varphi_1}{dt^2} \\
 M_Y - M_C &= J_2 \frac{d^2 \varphi_2}{dt^2}
 \end{aligned} \right\} \quad (2)$$

:

(            )      -

-

-

.(Huk)

:

$$J_2 \qquad \qquad \qquad J_1$$

(2)

:

$$\frac{d^2 M_Y}{dt^2} + \Omega_{12}^2 M_Y = \Omega_{12}^2 \left( \frac{M}{\gamma_2} + \frac{M_C}{\gamma_1} \right) \quad (3)$$

:  $\gamma_2, \gamma_1$

:

$$\gamma_2 = \frac{J_1 + J_2}{J_2}, \quad \gamma_1 = \frac{J_1 + J_2}{J_1}$$

(3)

:

$M_C J_2$

$$\left( \frac{M}{\gamma_2} + \frac{M_C}{\gamma_1} \right) = \varepsilon_{mid} J_2 + M_C \quad (4)$$

:

$$: \varepsilon_{mid} = \frac{M - M_C}{J_1 + J_2}$$

$$C_{12} = \infty$$

:

:  $\Omega_{12}$

$$\Omega_{12} = \sqrt{\frac{C_{12}(J_1 + J_2)}{J_1 \cdot J_2}}$$

$$: T = \frac{1}{\Omega_{12}}$$

(3) (4)

:

$$T^2 \frac{d^2 M_y}{dt^2} + M_y = \varepsilon_{mid} J_2 + M_C \quad (5)$$

:

$$(T^2 P^2 + 1) M_y = \varepsilon_{mid} J_2 + M_C \quad (6)$$

:

$$P_{1,2} = \pm j \Omega_{12}$$

$$M_y = \varepsilon_{mid} J_2 + M_C + A \sin \Omega_{12} t + B \cos \Omega_{12} t \quad (7)$$

$$M_y = A \sin \Omega_{12} t + B \cos \Omega_{12} t \quad (8)$$

$$: \quad (t = 0)$$

$$M_y = M_C, \quad \frac{dM_y}{dt} = 0$$

$$M_y = \varepsilon_{mid} J_2 (1 - \cos \Omega_{12} t) + M_C \quad (9)$$

$$. (9) \quad M_C = 0$$

$$\left. \begin{aligned} \omega_1 &= \varepsilon_{mid} t + \frac{\varepsilon_{mid}}{\Omega_{12}} \frac{J_2}{J_1} \sin \Omega_{12} t \\ \omega_2 &= \varepsilon_{mid} t - \frac{\varepsilon_{mid}}{\Omega_{12}} \sin \Omega_{12} t \end{aligned} \right\} M_y \quad (10)$$

(9)

$$: \quad M_{y(max)} \quad M_{y(min)}$$

$$2 \varepsilon_{mid} J_2 + M_C$$

Transfer function ( )

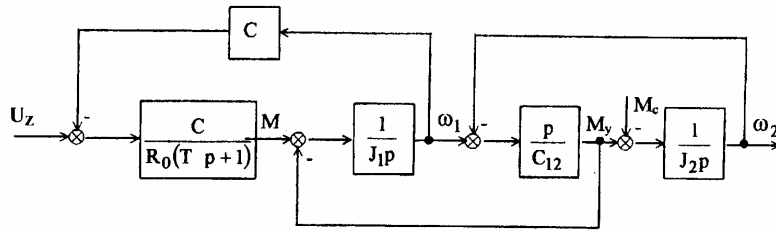
$$: \quad (2)$$

( $\beta$ )

$$M = M_k - \beta \omega_1 \quad (11)$$

$$\beta = \frac{M_k}{\omega_0} \quad ( \quad ) \quad : M_k$$

$$\omega_1 = \frac{M_k - M_y}{J_1 P + \beta} \quad (12)$$



(2)

(3)  $(\omega_1)$

$$(T^2 P^2 + 1)M_y = \frac{M_C}{\gamma_1} + \frac{M_k - \beta}{\gamma_2} \frac{M_k - M_y}{J_1 P + \beta} \quad (13)$$

$$H(P) = \frac{M_y(P)}{M_n(P)} = \frac{T_{m2}P}{T^2 T_M P^3 + T_2^2 P^2 + T_M P + 1} \quad (14)$$

$$: T_M = \frac{J_1 + J_2}{\beta}$$

$$: T_2 = \sqrt{\frac{J_2}{C_{12}}}$$

$$: T = \frac{1}{\Omega_{12}}$$

---


$$T_{m2} = \frac{J_1}{\beta}$$

$U_Z$

$H(P) \quad (\omega_2)$

:

$$H(P) = \frac{\omega_2(P)}{U_Z(P)} = \frac{K}{T_M T_{cm} T_2^2 P^4 + T_M T_2^2 P^3 + (T_2^2 \gamma_1 + T_M T_{cm}) P^2 + T_M P + 1} \quad (15)$$

:

$$: T_{em} = \frac{L_{a\Sigma}}{R_{a\Sigma}}$$

: (15)

$$T_M \cdot T_{cm} \cdot T_2^2 \cdot P^4 + T_M \cdot T_2^2 \cdot P^3 + (T_2^2 \cdot \gamma_1 + T_M \cdot T_{cm}) P^2 + T_M \cdot P + 1 = 0 \quad (16)$$

(16)

[8]



[5,6,7]

$$H(P) = \frac{K_1}{T_a T_M P^2 + T_M P + 1} \quad (17)$$

$K_1 = \frac{1}{K\phi} = \frac{1}{C}$   
 $C = K\phi$

$$K\phi = \frac{U_n - I_n R_a}{\omega_n}$$

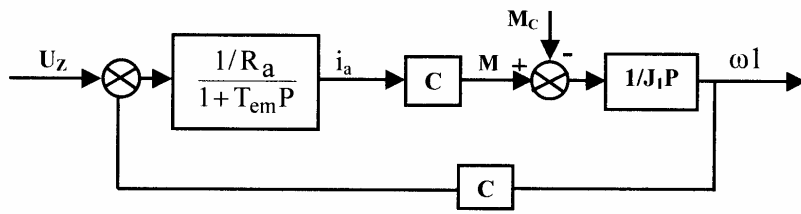
$T_a$   
 $T_M$

$T_M > 4 T_a$

$$H(P) = \frac{K}{T^2 P^2 + 2T\xi P + 1} \quad (18)$$

$T = \sqrt{T_a \cdot T_M}$

(3)



(3)

.ξ T

: (15)

$$H(P) = \frac{K}{a_0 P^4 + a_1 P^3 + a_2 P^2 + a_3 P + 1} \quad (19)$$

:

$$a_0 = T_{em} \cdot T_M \cdot T_2^2$$

$$a_1 = T_M \cdot T_2^2$$

$$a_2 = T_{em} \cdot T_M + T_2^2 \gamma_1$$

$$a_3 = T_M$$

(2)

(5)

:

.Kφ

:C

:Kco

:H<sub>1</sub>(P)

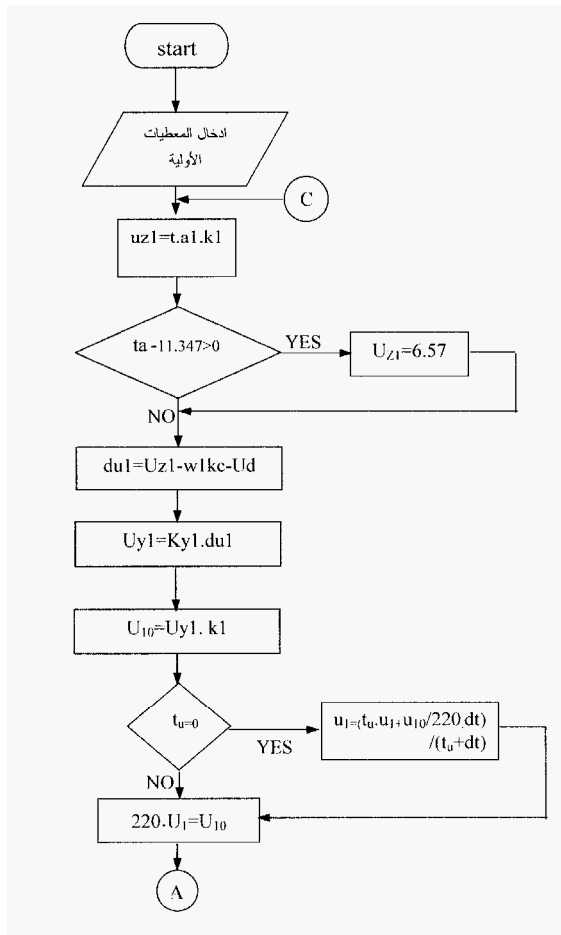
:H<sub>2</sub>(P)

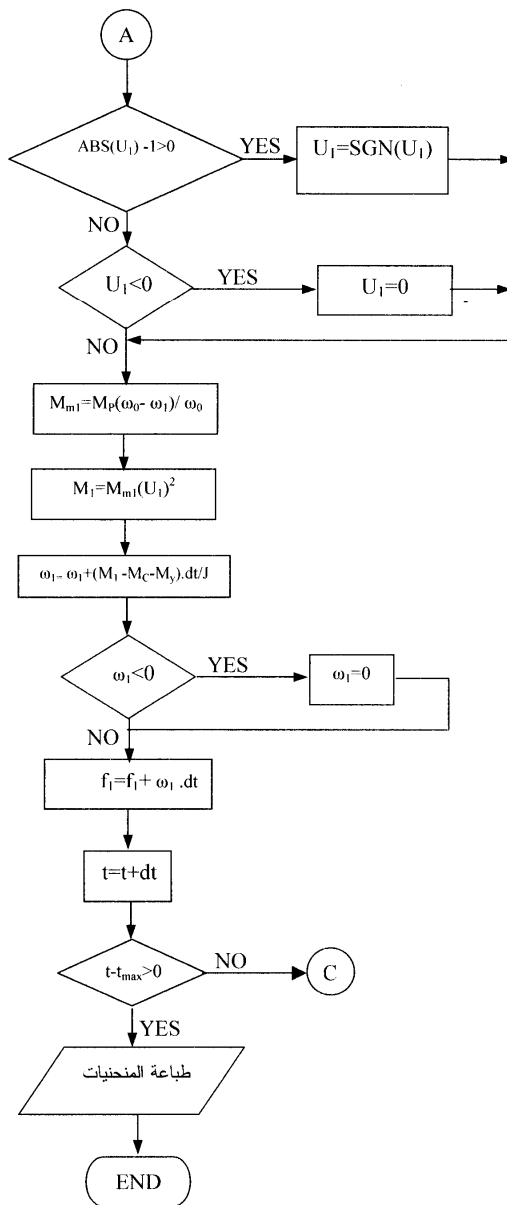
:H<sub>3</sub>(P)

:  $H_4(P)$

-2-3

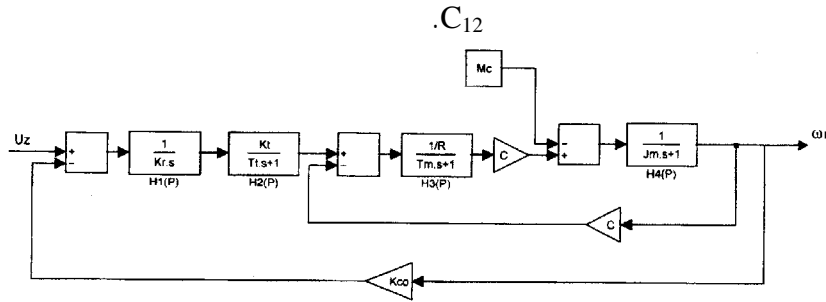
(4)





(4)

(5)  
SIMULINK



(simulink)

(5)

: -3-3

(10) (9)

$G = 76,5 \cdot 10^3 \text{ [kg]}$  -1

$V = 1,42 \text{ [m/sec]}$  -2

$a = 0,5 \text{ [m/sec}^2\text{]}$  -3

$M_C = 0,6 \text{ [M}_n\text{]}$  -4

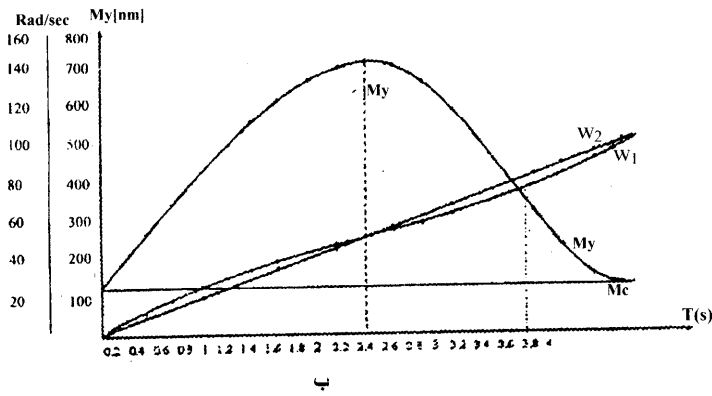
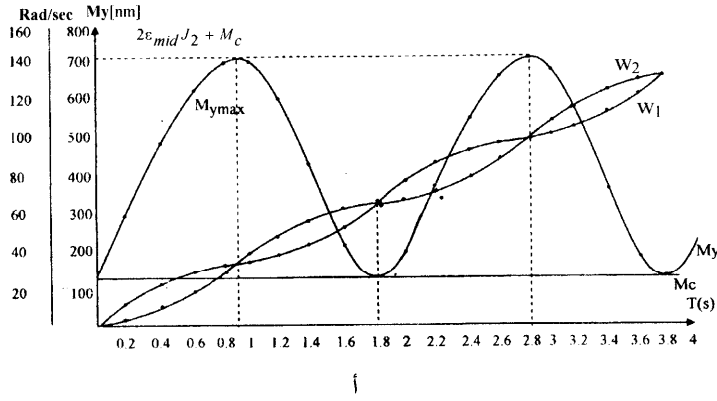
$U_n = 220 \text{ [V]}$  ,  $P_n = 27 \text{ [kW]}$  ,  $M_{max} = 630 \text{ [N.m]}$   
 $m = 280 \text{ [kg]}$  ,  $J_1 = 0,5 \text{ [kg m}^2\text{]}$  ,  $n = 950 \text{ [r.p.m]}$

$$\varepsilon_{mid} = 35 [m/sec^2] , J_2 = 7,77 [kg.m^2] ,$$

$$J_1 = 0,5 [kg.m^2] , \Omega_{12} = 88,47 [rad/sec]$$

(5) (6)

( $\omega_1$ ) ( $\omega_2$ )



$$C_{12} \quad - \quad (6)$$

$$5 C_{12} \quad -$$

(6)

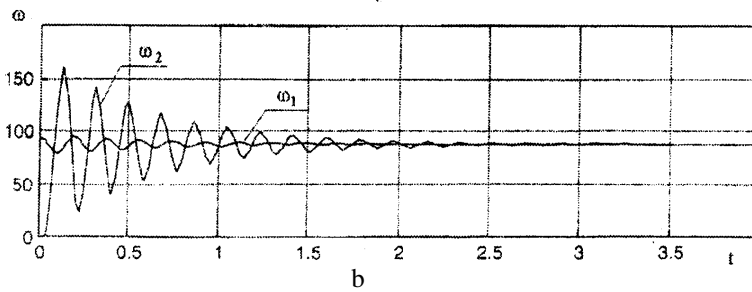
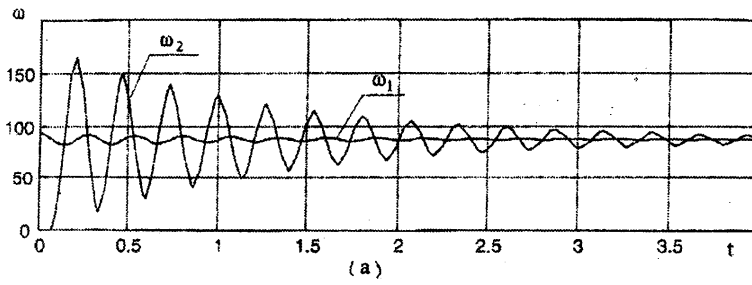
(7)

simulink

$$\omega_2 \quad \omega_1$$

$$(6)$$

(6)



(MATLAB) (7)

$$C_{12} = 0,5 \quad (C_{12}) = 85 \text{ N.m/rad} \quad -a :$$

$$C_{12} = (C_{12})_{opt} = 190 \text{ N.m/rad} \quad -b$$

$$\Omega_0 = \Omega_{12} \quad (20)$$

$$\therefore \Omega_0 = \frac{\sqrt{1-\xi^2}}{T} :$$

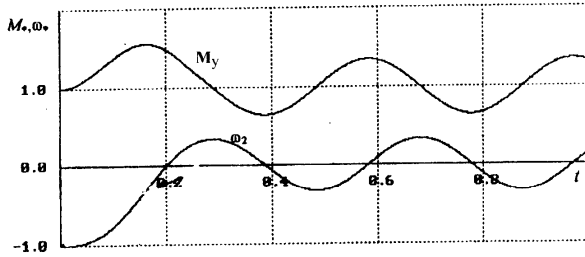
(20)

$T_a, T_M, J_1, J_2$

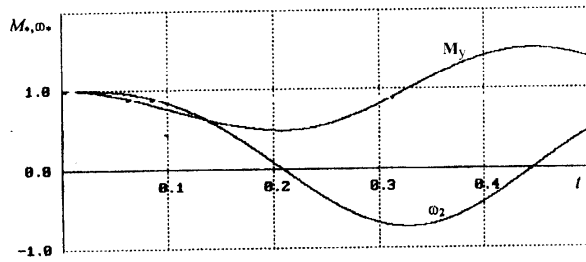
$C_{12}$

$C_{12}$

(8)



a



(8)

$l = 15 m \quad -a$

$l = 30 m \quad -b$

$(\Omega_{12}) \quad (\Omega_0)$

$C_{12}$



$$(C_{12})_{\text{opt}} = \frac{J_1 \cdot J_2 (T_a - 0,25 \cdot T_m)}{T_a^2 \cdot T_m (J_1 + J_2)} \quad (21)$$

(19) (1)

$$\left. \begin{aligned} P_{1,2} &= -\alpha_1 \pm j\Omega_{01} \\ P_{3,4} &= -\alpha_2 \pm j\Omega_{02} \end{aligned} \right\} \quad (22)$$

:  $(\alpha_1, \alpha_2)$

:  $(\Omega_{01}, \Omega_{02})$

(2)  
 $H_1(P)$

$$\left. \begin{aligned} H_1(P) &= \frac{K_1}{T_1^2 P^2 + 2T_1 \xi_1 P + 1} \\ H_2(P) &= \frac{K_2}{T_2^2 P^2 + 2T_2 \xi_2 P + 1} \end{aligned} \right\} \quad (23)$$

$(T_2 \ \& \ T_1)$

$(\xi_2, \xi_1)$

$$\xi_2 = \alpha_2 T_2 \quad , \quad \xi_1 = \alpha_1 T_1 \quad :$$

---


$$T_2 = \frac{1}{\sqrt{\Omega_{02}^2 + \alpha_2^2}} \quad , \quad T_1 = \frac{1}{\sqrt{\Omega_{01}^2 + \alpha_1^2}}$$

$$K_2 = 1 \quad , \quad K_1 = \frac{1}{C} = \frac{1}{K\phi}$$

[8]

:

$$\alpha_1 = \frac{\beta}{2J_1} \quad , \quad \alpha_2 = \frac{\beta}{2J_2}$$

$$\Omega_{01} = \sqrt{\frac{\beta^2}{4J_1^2} - \frac{C_{12}}{J_1}} \quad , \quad \Omega_{02} = \sqrt{\frac{\beta^2}{4J_1^2} - \frac{C_{12}}{J_2}}$$

( $\beta$  const)

( $J_1 \ll J_2$ )

( $\alpha_1$ )

-

[7]

-

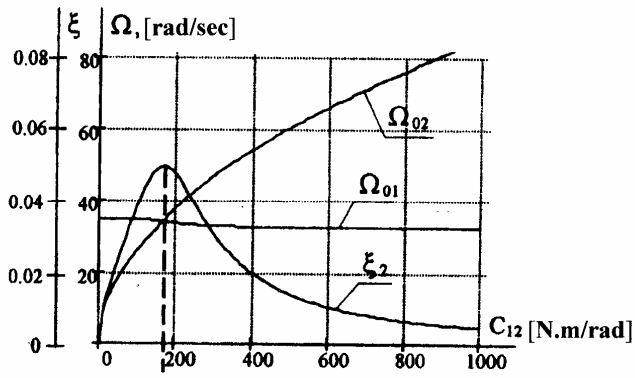
(2)

$C_{12}$

( $\xi$ ) ( $\Omega_{01}, \Omega_{02}$ )

(P<sub>3,4</sub>)

(9)



(9)

(1000 N.m)

(9)

( )

$\cdot C_{12}$

$(J_2, J_1, \beta)$

$C_{12}$

$(\Omega_{01} = \Omega_{02})$

(9)

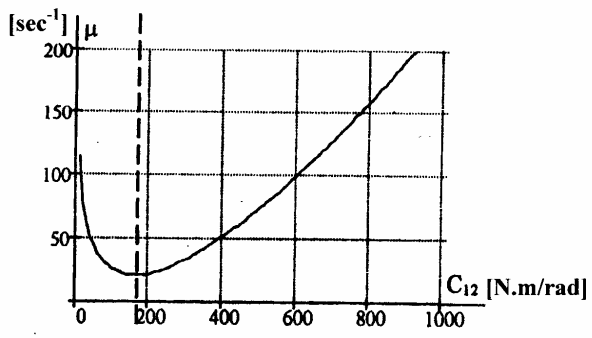
(200 N.m)

(21)

(9)

$\cdot C_{12}$

$(\mu)$



( $C_{12}$ )

(10)

(10)

(9)

( $\mu$ )

(190 N.m/rad)

(8)

:

:

-1

-

.( $C_{12}$ )

-2

:

.( $\Omega_{01} = \Omega_{02}$ )

-

-3

$$(8) \quad (M_y = M_{12})$$

.(2)

$$(\Omega_{02})$$

-4

$$( \quad )$$

-5

$$(C_{12})$$

:

$$(\Omega_{01} = \Omega_{02})$$

$$( \quad )$$

.(10) (9)

:

$$( \quad )$$

$$( \quad )$$

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