

. Riccati

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	:		-1
		$\Delta$	
		$\bullet = d/dt$	
		$\delta$	$\omega$
		$e'_q$	
		M, D	
		$V_t$	
		$E_{fd}$	
		$K_A, T_A$	
		$V_{ref}$	
		U	
		$T'_{do}$	
	$K_1, K_2, \dots, K_6$		
50		f	
		s	
		$x_d, x_q$	
		$x'_d$	
		$R_l, x_l$	
		$G_l, B_l$	
		$P_G, Q_G$	

: -2

:

. [11,12,13]

. [1,2,3]

: [4,5]

: Inter-tie mode •

0.2-0.5 Hz

.....

• Local mode :

0.8-1.8 Hz

• Intra-system mode :

3-6 Hz

. [6] exciter mode

. (stabilizer)

(1) :

(2)

. (Riccati)

: -3

$$\dot{X} = AX + BU \quad (1)$$

U X B A

(1)

: [7]

$$\dot{\Delta\delta} = 2\pi f \Delta\omega \quad (2)$$

$$\dot{\Delta\omega} = -\frac{K_1}{M} \Delta\delta - \frac{D}{M} \Delta\omega - \frac{K_2}{M} \Delta e'_q \quad (3)$$

$$\dot{\Delta e}'_q = -\frac{K_4}{T'_{do}} \Delta\delta - \frac{1}{K_3 T'_{do}} \Delta e'_q + \frac{1}{T'_{do}} \Delta E_{fd} \quad (4)$$

$$\Delta V_t = K_5 \Delta\delta + K_6 \Delta e'_q \quad (5)$$

$$\dot{\Delta E}_{fd} = -\frac{K_A K_5}{T_A} \Delta\delta - \frac{K_A K_6}{T_A} \Delta e'_q - \frac{1}{T_A} \Delta E_{fd} + \frac{K_A}{T_A} U + \frac{1}{T_A} \Delta V_{ref} \quad (6)$$

:

.....

$$\begin{bmatrix} \dot{\Delta\delta} \\ \dot{\Delta\omega} \\ \dot{\Delta e'_q} \\ \dot{\Delta E_{fd}} \end{bmatrix} = \begin{bmatrix} 0 & 2\pi f & 0 & 0 \\ -\frac{K_1}{M} & -\frac{D}{M} & -\frac{K_2}{M} & 0 \\ -\frac{K_4}{T_{do}} & 0 & -\frac{1}{K_3 T_{do}} & \frac{1}{T_{do}} \\ 0 & 0 & -\frac{K_4 K_6}{T_A} & -\frac{1}{T_A} \end{bmatrix} \begin{bmatrix} \Delta\delta \\ \Delta\omega \\ \Delta e'_q \\ \Delta E_{fd} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{K_A}{T_A} \end{bmatrix} \Delta V_{ref} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{K_A}{T_A} \end{bmatrix} U$$

(7)

$$\begin{aligned} \dot{X} &= [\Delta\delta \quad \Delta\omega \quad \Delta e'_q \quad \Delta E_{fd}]^T \\ U &= 0 \end{aligned}$$

[8]

(2)

(2)

:

$$\frac{E_o(s)}{E_i(s)} = K_c \left( \frac{s + \frac{1}{T}}{s + \frac{1}{\alpha T}} \right) \quad (8)$$

$$K_c = \frac{R_4 C_1}{R_3 C_2}, \quad \alpha T = R_2 C_2, \quad \alpha = \frac{R_2 C_2}{R_1 C_1}, \quad T = R_1 C_1 :$$

$$R_1 C_1 > R_2 C_2 \quad \alpha < 1$$

(1)

(4)

: (4)

$$\dot{\Delta X} = -K_5 \Delta \delta - K_6 \Delta e'_q - \frac{1}{\alpha T} \Delta X_5 + \Delta V_{ref} + U \quad (9)$$

:

$$\dot{\Delta E}_{fd} = -\frac{K_c K_5 K_A}{T_A} \Delta \alpha - \frac{K_c K_6 K_A}{T_A} \Delta e'_q + \frac{K_c K_A}{T_A} \left( \frac{1}{T} - \frac{1}{\alpha T} \right) \Delta X_5 - \frac{1}{T_A} \Delta E_{fd} + \frac{K_c K_A}{T_A} \Delta V_{ref} + \frac{K_c K_A}{T_A} U$$

(10)

10 9 4 3 2

:

$$\begin{bmatrix} \dot{\Delta \delta} \\ \dot{\Delta \omega} \\ \dot{\Delta e}'_q \\ \dot{\Delta X}_5 \\ \dot{\Delta E}_{fd} \end{bmatrix} = \begin{bmatrix} 0 & \frac{2\pi f}{D} & 0 & 0 & 0 \\ -\frac{K_1}{M} & -\frac{1}{M} & -\frac{K_2}{M} & 0 & 0 \\ -\frac{K_4}{T'_{do}} & 0 & -\frac{1}{K_3 T'_{do}} & 0 & \frac{1}{T'_{do}} \\ -K_5 & 0 & -K_6 & -\frac{1}{\alpha T} & 0 \\ -\frac{K_c K_5 K_A}{T_A} & 0 & -\frac{K_c K_6 K_A}{T_A} & \frac{K_c K_A}{T_A} \left( \frac{1}{T} - \frac{1}{\alpha T} \right) & -\frac{1}{T_A} \end{bmatrix} \begin{bmatrix} \Delta \delta \\ \Delta \omega \\ \Delta e'_q \\ \Delta X_5 \\ \Delta E_{fd} \end{bmatrix} \quad (11)$$

$$+ \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{1}{T_A} \\ \frac{K_c K_A}{T_A} \end{bmatrix} \Delta V_{ref} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{1}{T_A} \\ \frac{K_c K_A}{T_A} \end{bmatrix} U$$

(11)

$$X = [\Delta \delta \quad \Delta \omega \quad \Delta e'_q \quad \Delta X_5 \quad \Delta E_{fd}]^T$$

.U=0

: [9,10] U

$$J = \frac{1}{2} \int_0^{\infty} (X^T Q X + U^T R U) dt$$

(12)

: X

$$U = -kX = -R^{-1} B^T P X \quad (13)$$

P k R Q

Riccati

: [7,9,14]

$$A^T P + P A - P B R^{-1} B^T P + Q = 0 \quad (14)$$

:

$$\dot{X} = (A - B R^{-1} B^T P) X + B U \quad (15)$$

:

**-4**

:

. [IEEE TYPE-1]

**: [7] [p.u.]**

$$x_d = 1.6$$

$$x'_d = 0.17$$

$$x_q = 1.53$$

$$M = 4.74$$

$$D = 0.0$$

$$T'_{do} = 7.76$$

:

$$K_A = 200$$

$$T_A = 0.05$$

:

$$R_l = -0.02$$

$$x_l = 0.40$$

$$G_l = 0.249$$

$$B_l = 0.262$$



$P_G = 1.0$   
 $V_t = 1.0$

:  
 $Q_G = 0.62$   
 $f = 50$  [Hz]

[7,11]  $K_1, K_2, \dots, K_6$

$K_1 = 1.075$   
 $K_4 = 1.777$

$K_2 = 1.344$   
 $K_5 = -0.0162$

$K_3 = 0.3014$   
 $K_6 = 0.5891$

Riccati

U

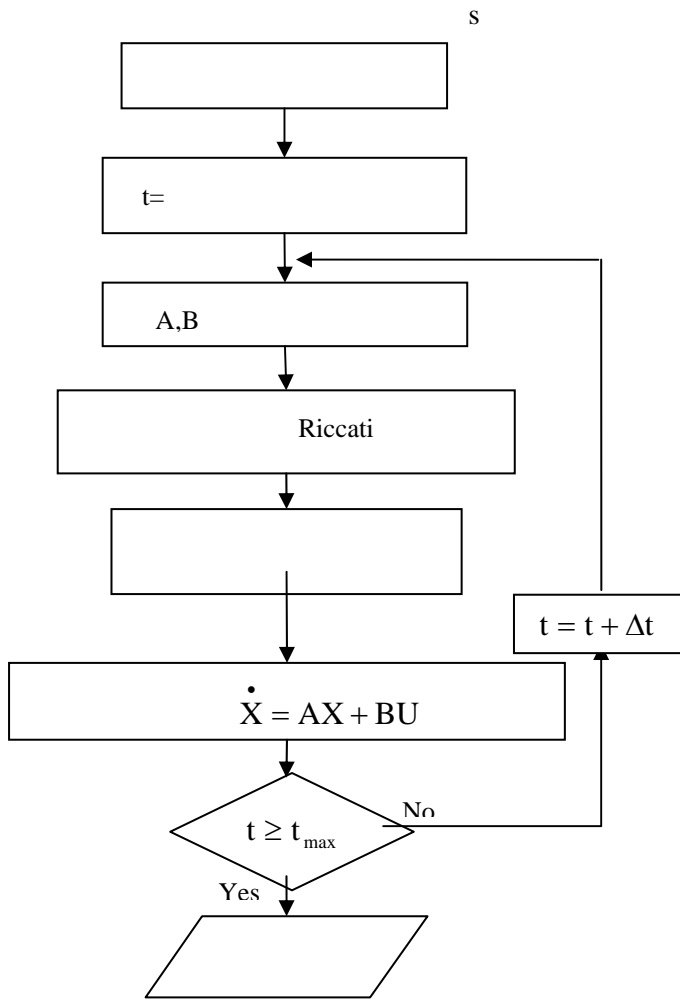
Excel

1 0.1 p.u.

:

.1  
.2  
.3

(1)



(7) (6) (5)

$$\dot{\Delta V}_t \quad \Delta \omega \quad \Delta \delta$$

(1)

$\Delta \delta$

(10) (9) (8)

$$\Delta V_t \quad \Delta \omega$$

$K_c = 1.0, \quad \alpha = 0.054, \quad T = 0.245 :$

(1)

3

(13) (12) (11)

$$\Delta \omega \quad \Delta \delta \quad U$$

(14)

(11)

$$\Delta V_t$$

:

Riccati

$$U = 0.125\Delta\delta - 5.383\Delta\omega + 0.299\Delta e'_q + 5.163\Delta X_5 + 0.004\Delta E_{fd}$$

R Q

$$R=[1]$$

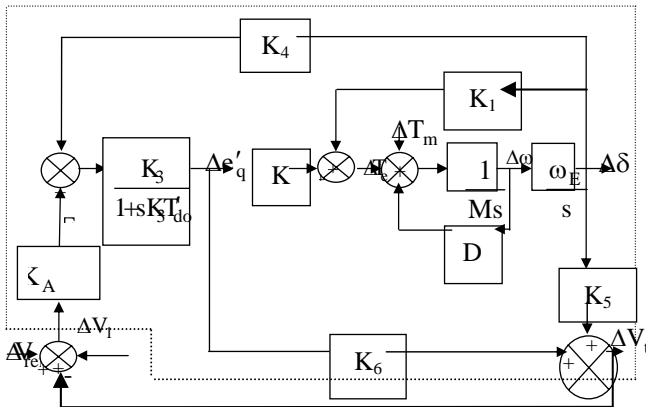
$$Q=[0.051 \quad 0.001 \quad 0.001 \quad 20.001 \quad 0.0001]^T$$

.....

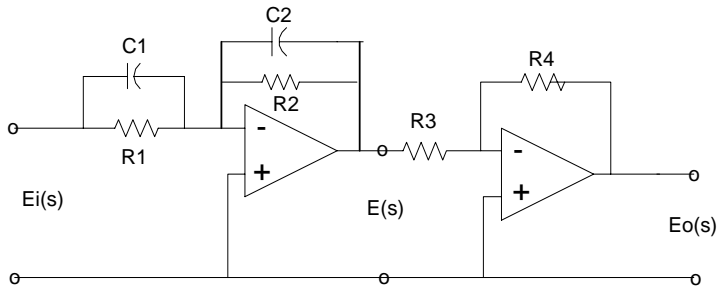
(1)

	-	
-92.017 -21.631 -0.372±j8.453 -0.915	-69.808 -25.141 -0.106±j8.439 -0.853	-10.28±j14.446 0.067±j8.477

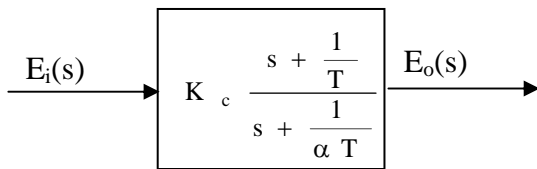
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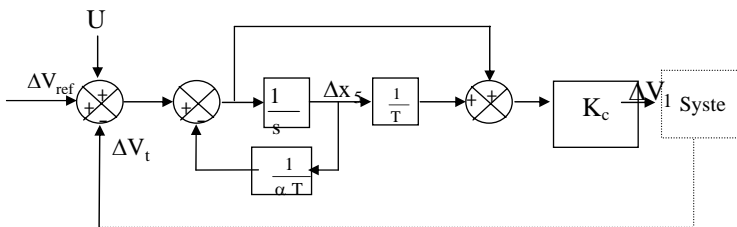
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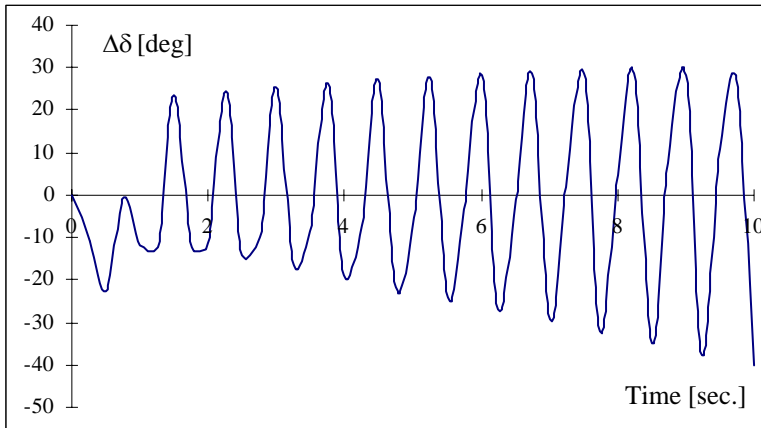
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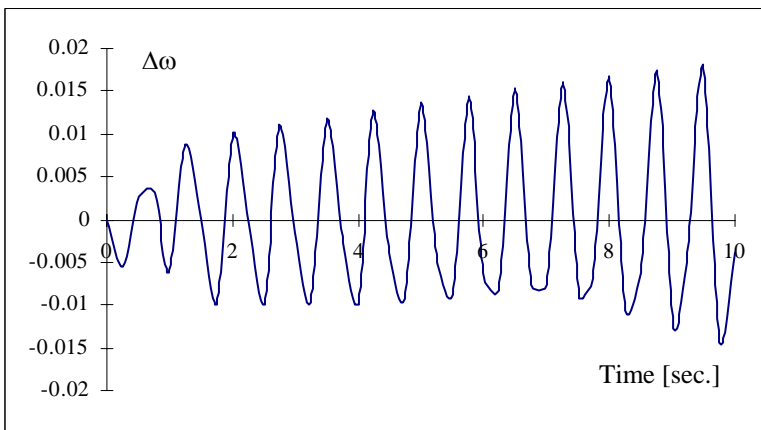
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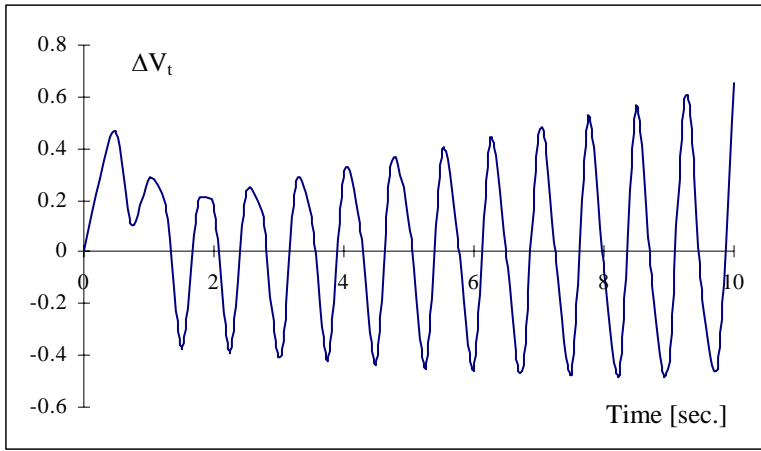
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(5)

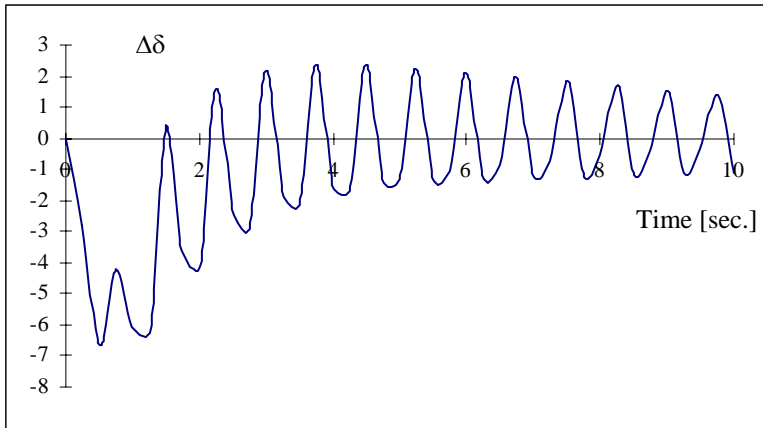


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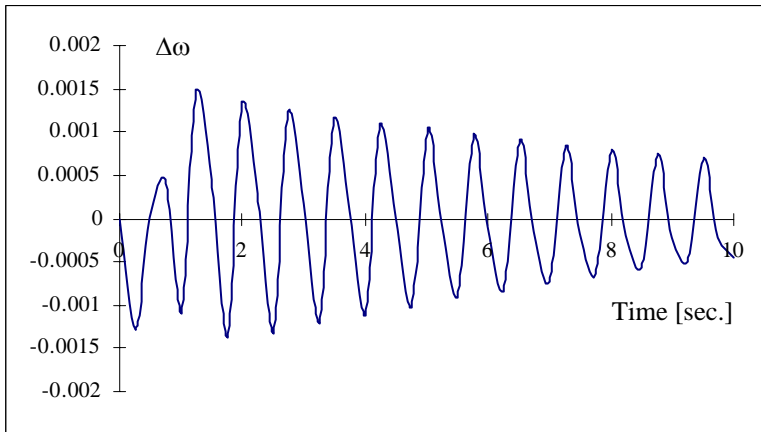


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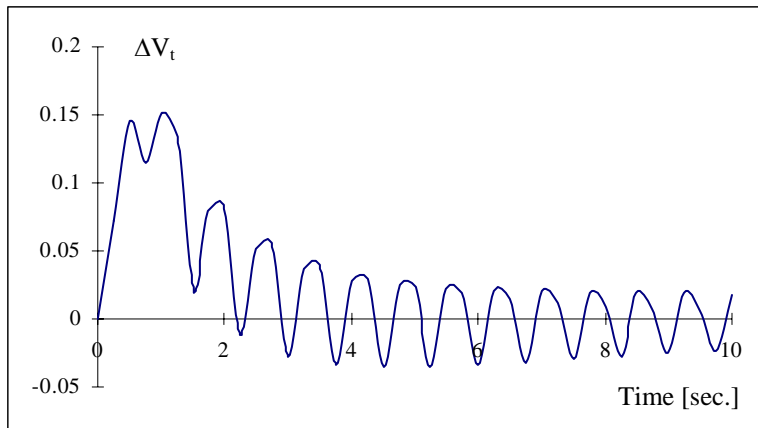


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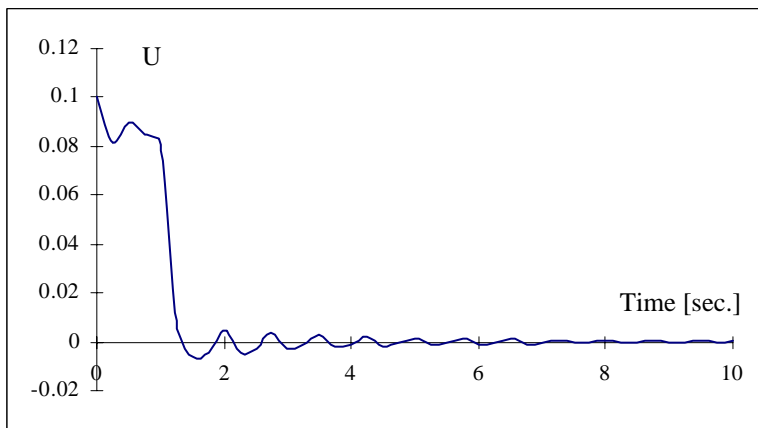


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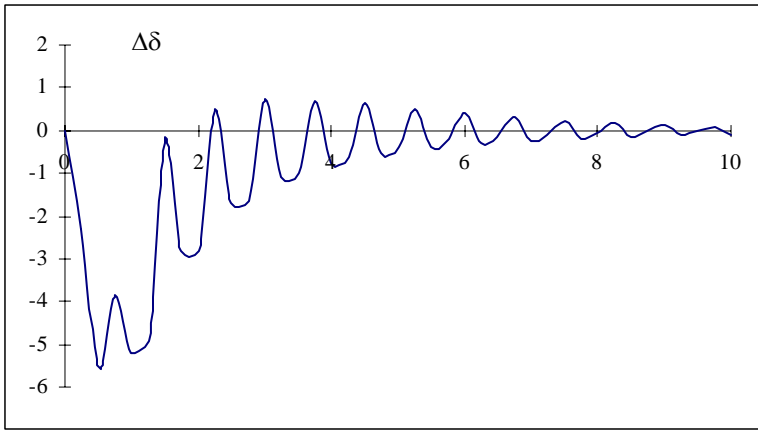




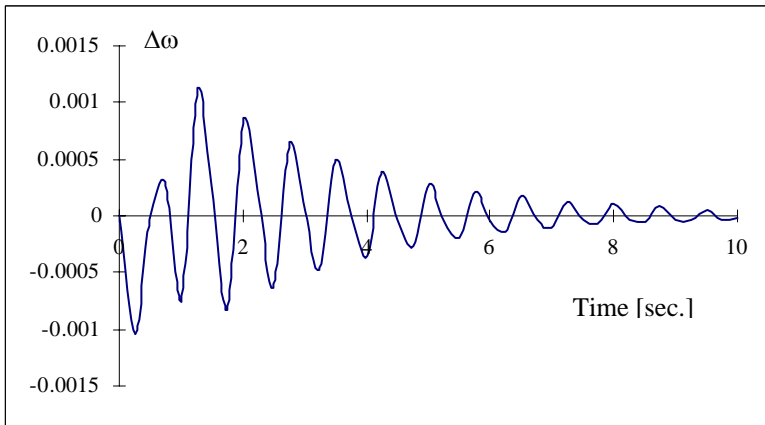
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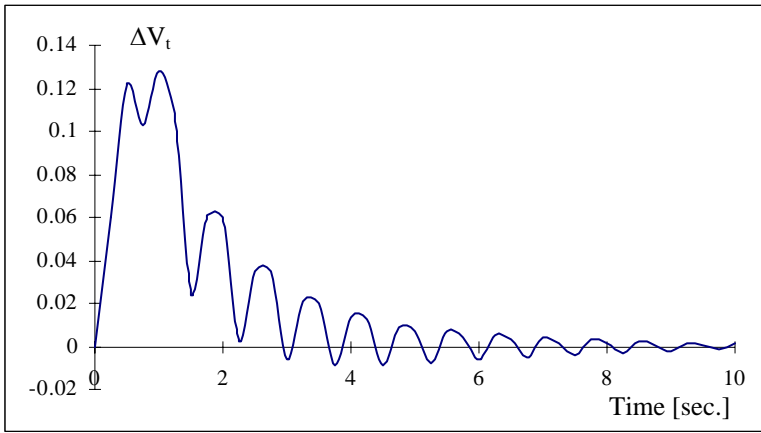
(11)



(12)



(13)



(14)

- [1]-de Mello, F. P. and T.F. Laskowski, "Concepts of Power System Dynamic Stability", IEEE Trans. On Power Apparatus and Systems, Vol. PAS-94, 1979, pp.827-833.
- [2]-Dandeno, P. L. , A. N. Kars, K. R. McClymont and W. Waston, "Effect of High-Speed rectifier excitation System on Generator Stability Limits", IEEE Trans. On Power Apparatus and Systems, Vol. PAS-87, 1968, pp. 190-200
- [3]- Hoa Vu., J. C. Agee, " Comparison of Power System Stabilizers for Damping Local Mode Oscillations" IEEE Trans. On Energy Conversion, Vol. 8, No. 3, September 1993, pp 533-538.
- [4]- E .V . Laresen and D . A . Swan ' Applying power system stabilizers ' part I , II , III , IEEE Trans . vol . PAS -100 , No. 6 June 1981 pp 3017 – 3046
- [5]- P . Kundur , M . Klein , G . J . Rogers and M . S . Zywo ' Application of power system stabilizers for enhancment of overall system stability ' , ibid , vol . 4 , No. 2 , May 1989 , pp 614 -621 .
- [6]- P . Kundur , D . C . Lee H . M . Zein El - Din , " Power system stabilizers for thermal units : Analytical techniques and on - site validation " , IEEE Trans. , vol. PAS -100 , No. 1 , January 1981 , pp 81 - 95 .

- [7]- Yu . , Y. N . , ‘ Elecric power system dynamics ‘ , Academic Pres , INC . U . S . A , 1983 .
- [8]- K . Ogata, ‘Modern control engineering ‘ Prentice-Hall, INC, 1990.
- [9]- G . P. Chen. , O. P. Malik, Y . H . Qin and G. Y. Xu. , ‘ Optimization technique for the desgin of a linear optimal power system stabilizer‘ IEEE Trans. on energy conversion, vol. 7, No. 3, september 1992, pp 453 -459.
- [10]- Yuan-chyuan Lee, Chi-Jui Wu, ‘Damping of Power System Oscillations with output feedback and Strip Eigenvalues Assignment’ , IEEE Trans. On Power Systems, Vol. 10, No. 3 august 1995.
- [11]- Peter w. Saver, M. a. PAI, " Power System Dynamics and stability " Prentice Hall, Inc. 1998.
- [12]- J. Machowski, J. Bialek, J. R. Bumby, " Power System Dynamics and Stability ", John Wiley & sons Ltd. , 1997.
- [13]- M. Pavella, P. G. Murthy, " Transient stability of Power System ", John Wiley & Sons Ltd. 1994.
- [14]- Jeffery B. Burl, " Linear Optimal Control ", Addison- Wesley, Inc 1999.\*

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